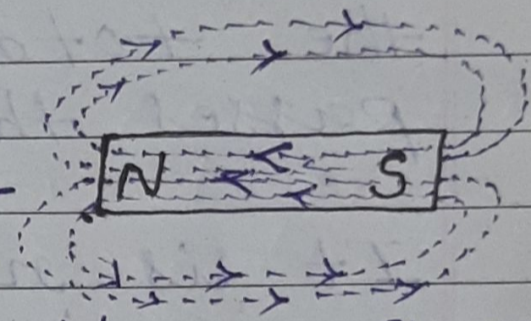


\* magnetic circuit :- It is a closed path formed by magnetic material through which the magnetic flux can be transferred is known as magnetic flux.

OR

magnetic line of force originate from north-pole & terminate to the south-pole in outside the magnet, and inside the magnet south-pole to north-pole.



- magnetic fields of line makes always a closed loop.

\* magnetic flux :- It is the magnetic line of forces originating from the unit north-pole of a magnet. It is denoted by  $\phi$ . Its unit is webers (wb).

$$1 \text{ wb} = 10^8 \text{ Maxwell (line of force)}$$

$$1 \text{ Maxwell} = 10^{-8} \text{ weber.}$$

\* It is analogous to current in electric circuit.

Analogous → same behaviour but different products element

OR

Magnetic flux is define as the number of magnetic field line passing through a given surface. It provides the measurement of the total magnetic field that passes through a given surface.

It is represented by  $\phi$  (Pie). Its unit is weber (wb).

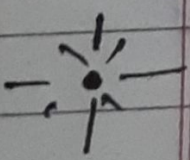
$$\phi = BA \cos \theta$$

where,

$B$  = magnetic field density.

$A$  = given area.

$\theta$  = Angle between surface and magnetic flux.



Flux Density :- It is the amount of flux per unit surface area of any magnetic material. It is denoted by 'B'

$$B = \frac{\phi}{A}$$

unit :-  $\frac{\text{weber}}{\text{m}^2}$  or tesla

\* Magnetic lines of force :-

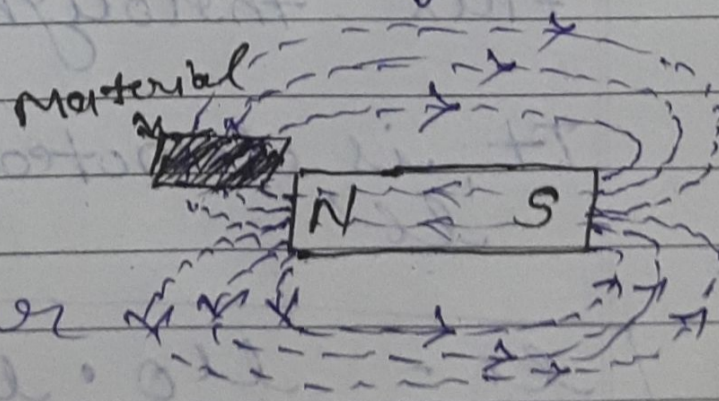
The magnetic lines of force are imaginary lines to represent magnetic field.

\* Magnetic field :- The region surrounding the magnet in which a piece of iron would experience a force is called magnetic field.

\* Magnetizing force or magnetic field intensity :-

It is the force experienced by a magnetic material placed near the unit north pole of a magnet. It is denoted by 'H'

$$H = \frac{NI}{l}$$



where,

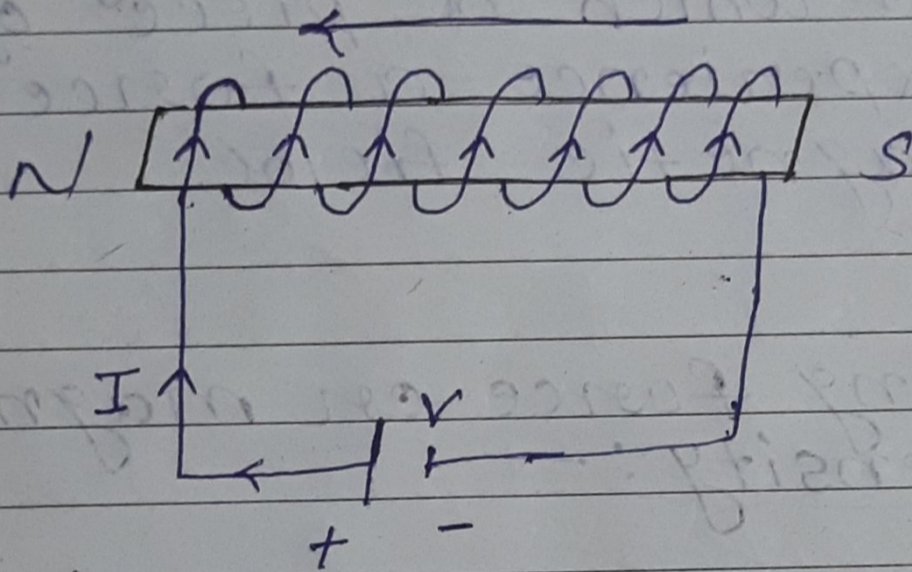
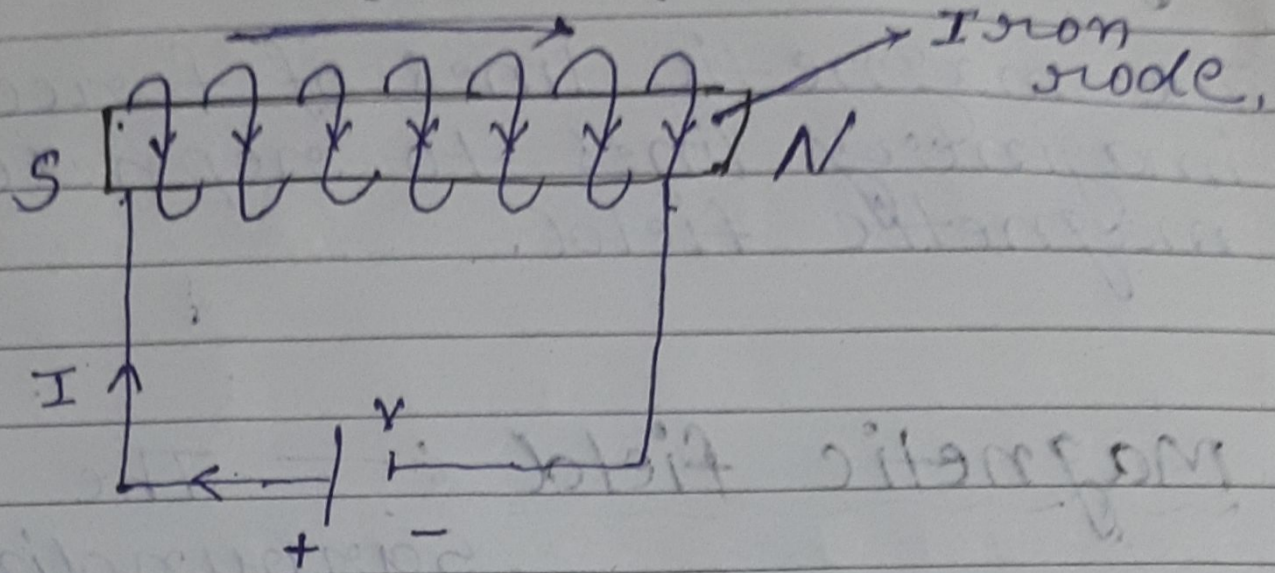
N = No. of conductor turns

I = supply current

l = length of conductor

\* Unit :- Ampereturns (AT/m)

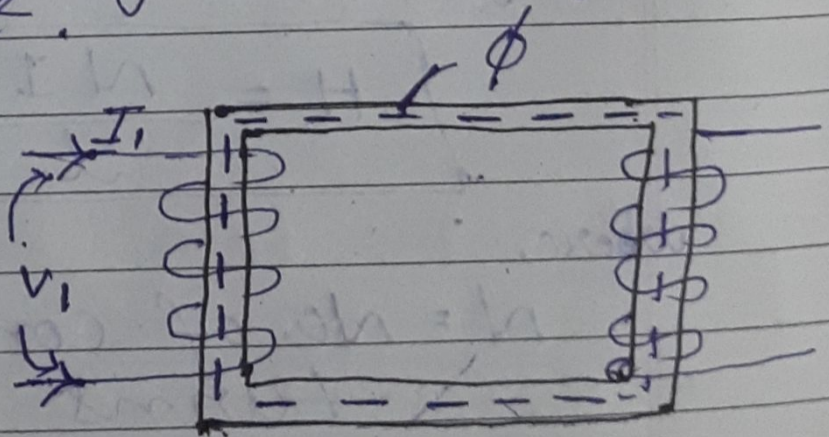
\* Electro magnet \*



\* permeability: - It is ability of a magnetic material to allow the passage of magnetic flux through it.

It is denoted by 'μ'

$$\mu = \mu_0 \cdot \mu_r$$



$\mu_0$  = Absolute permeability.

$(4\pi \times 10^{-7})$  unit  $\rightarrow$  Henry per meter

$$e = \frac{1}{\mu_0} \frac{N d \phi}{dt}$$

$\mu_r$  = Relative permeability of medium

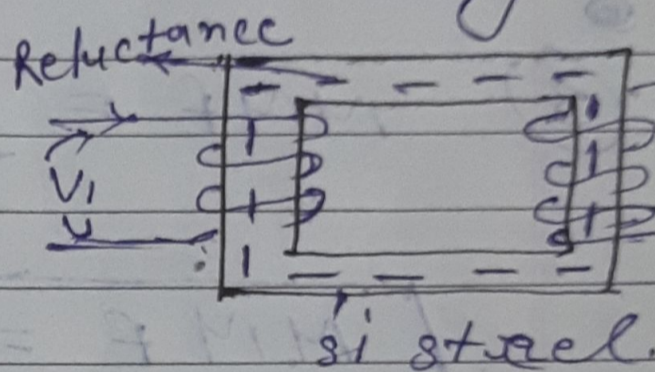
$\mu_r = 1$  { only for air or vacuum }

\* It is unit less quantities.

\* Reluctance :- It is the opposition offered to the transfer of magnetic flux through a magnetic material. It is denoted by 'S'

$$S = \frac{1}{\mu} \cdot \frac{l}{A}$$

$$S \propto l, S \propto \frac{1}{A}$$



$$S = \frac{l}{A \mu_0 \mu_r} \rightarrow \text{unit} \rightarrow \frac{AT}{\text{weber}}$$

\* MMF (Magneto-motive-force) :-

It is the driving force required for the transfer of Magnetic material

$$MMF = \phi S \quad \because S = \frac{l}{A \mu_0 \mu_r}$$

$$\therefore MMF = \frac{\phi l}{\mu_r \mu_0} = \frac{B \cdot l}{\mu_r \mu_0}$$

$$\therefore \boxed{MMF = \frac{B l}{\mu_0 \mu_r}} \quad \text{--- (1)}$$

$$\therefore B \propto H$$

$$B = \mu H \quad \text{or} \quad B = \mu_0 \mu_r H$$

$$\text{or} \quad H = \frac{B}{\mu_0 \mu_r}$$

$$\textcircled{2} \quad \boxed{MMF = H \cdot l} \rightarrow \text{unit :- } \textcircled{AT}$$

we know that  $H = \frac{NI}{l}$

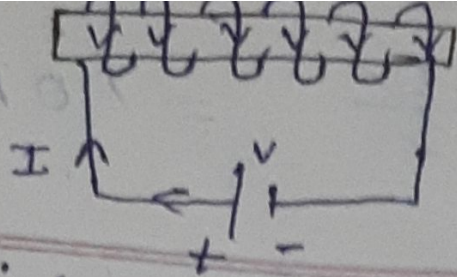
$$\textcircled{3} \quad MMF = \frac{N \cdot I}{l} \times l$$

$$\boxed{MMF = N \cdot I} \quad \text{unit :- } \textcircled{AT}$$

OR

\* MMF (Magneto Motive force) :-

MMF similar to the way that emf drives a current of electrical charge in electric circuits. MMF drives magnetic flux through the magnetic circuit.



- MMF is analogic (similar) of emf
- It is represented by "F"

$$\boxed{\text{MMF} = N \cdot I} \quad \text{unit} \rightarrow \text{AT}$$

where,

$N \rightarrow$  Number of turns

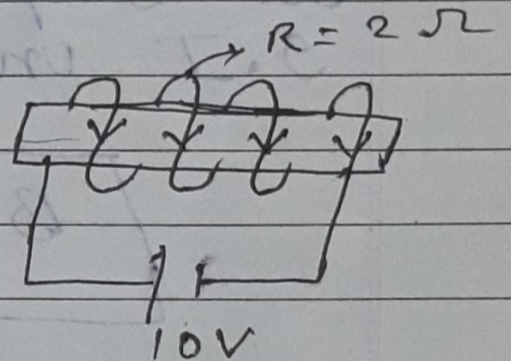
$I \rightarrow$  current flowing the turns.

Numericals.

Q: -

given,

$R = 2 \Omega$  ,  $N = 4$   
 $V = 10V$  ,  $\text{MMF} = ?$



$$I = \frac{V}{R} = \frac{10}{2} = 5A$$

$$\text{MMF} = N \cdot I = 4 \times 5 = 20 \text{ AT}$$

Ans.

Q: - If in a coil connected with a 20V DC source and resistance of the coil is  $2 \Omega$  then what will be the MMF generated by coil ( $N = 100$ )

given,  $V = 20V$  ,  $R = 2 \Omega$  ,  $N = 100$   
MMF = ?

$$I = \frac{V}{R} = \frac{20}{2} = 10 \text{ A}$$

$$\text{MMF} = N \cdot I$$
$$= 100 \times 10 = 1000 \text{ AT}$$

\* Magnetic field density :-

Magnetic field density is defined as the force acting per unit current per unit length on a wire placed at right angle to the magnetic field. It is a vector quantity. It is represented by 'B'. Its S.I unit is weber/m<sup>2</sup> or Tesla.

$$B = \frac{F}{IL} \quad \text{unit} \rightarrow \text{wb/m}^2 \text{ or Tesla.}$$

$$F = BIL$$

Q:- If a wire of length 5 cm kept in a magnetic field of value 0.5 Tesla at right angle and current flowing through the wire is 2 A then what will be the force acting on the wire.

→ given,  $L = 5 \text{ cm} = \frac{5}{100} \text{ m}$

$B = 0.5 \text{ T}$

$I = 2 \text{ A}$

$f = ?$

$$f = BIL$$

$$= \frac{0.5}{100} \times 2 \times \frac{5}{100}$$

$$f = 0.05 \text{ N}$$

Ans

\* Electro motive force (e.m.f): -

The electro motive force (e.m.f)

\* Potential difference :-

The potential difference (P.d) between two points in the energy required to move one coulomb of charge from one to the other.

$$V = \frac{W}{Q} \quad \text{unit} = \frac{J}{C}$$

where,

$W$  = energy required to transfer the charge

$Q$  = charge transferred between the points

$V$  = potential difference.

\* absolute permeability :-

The permeability of all non-magnetic materials including air is represented by is called Absolute permeability. It is denoted by  $\mu_0$ . Its unit is H/m.

$$\mu = \mu_0 \mu_r$$

$$\Rightarrow \mu_0 = \frac{\mu}{\mu_r}$$

$\mu_r$  = Relative permeability

$\mu$  = permeability.

\* Relative magnetic permeability:-

The degree or extent to which magnetic field can permeate a material is called Relative magnetic permeability. It is denoted by  $\mu_r$ . It has no dimension and unit.

$$\mu_r = \frac{\mu}{\mu_0}$$

OR

Relative magnetic permeability is the ratio of magnetic permeability of the material ( $\mu$ ) to the magnetic permeability of the free space ( $\mu_0$ )

$\mu_r$   $\left\{ \begin{array}{l} \text{for air or vacuum} = 1 \\ \text{for soft iron} = 8000 \end{array} \right.$

\* Reluctance :- The resistance offered by a magnetic circuit to the magnetic flux is known as Reluctance. As in electric circuit the reluctance is similar in the magnetic circuit.

OR

\* Reluctance is the ratio of mmf to the flux. Its SI unit is AT/Wb. It is represented by 'S'

$$S = \frac{\text{mmf}}{\text{Flux}} \quad \text{unit!} = \boxed{\text{AT/Wb}}$$

$$S = \frac{N \cdot I}{\phi}$$

$$S = \frac{l}{\mu_0 \mu_r A}$$

where,  $\mu_0 \rightarrow$  absolute permeability  
 $\mu_0 = 4\pi \cdot 10^{-7} \text{ H/m}$

$\mu_r \rightarrow$  relative permeability  
 $A \rightarrow$  crosssectional area of the

$l \rightarrow$  length of Rod.

\* Faraday law of electro magnetic Induction or Faraday's law:-

Michael Faraday proposed the law of electromagnetic induction in the year 1831.

Faraday law of electromagnetic induction consists of two laws. The first law describes the induction of emf in a conductor and the second law tells us the amount of emf induced.

\* Faraday's first law of electromagnetic induction:-

Whenever a conductor is placed in a varying (change) magnetic field, an electromotive force (emf) is induced. If the conductor circuit is closed, a current is induced.

\* faraday's first law of electro-magnetic induction :-

Whenever a conductor is placed in a varying (change) magnetic field. An electromotive force (emf) is induced. If the conductor circuit is closed a current is induced it is called induced current.

\* faraday's second law of electro-magnetic induction :-

faraday's second law state that the emf produce due to electromagnetic induction is directly proportional to rate of change of flux with respect to time and no. of turns of the conductor

$$e \propto \frac{N d\phi}{dt}$$

$$e = \frac{N d\phi}{dt} \quad \text{unit} = \frac{\text{WT}}{\text{sec}}$$

• constant values is 1.

## \* Lenz's Law :-

Lenz's law states that the direction of the electric current induced in a conductor by a changing magnetic field such that the magnetic field created by the induced current opposes in the initial magnetic field.

$$e = -N \frac{d\phi}{dt}$$

Negative stand for Lenz law

\* It is the combination of Faraday second law and Lenz law.

## \* Self Induction :-

It is the phenomenon due to ~~the~~ which an emf induced in a coil as a result of change in current flowing through it.

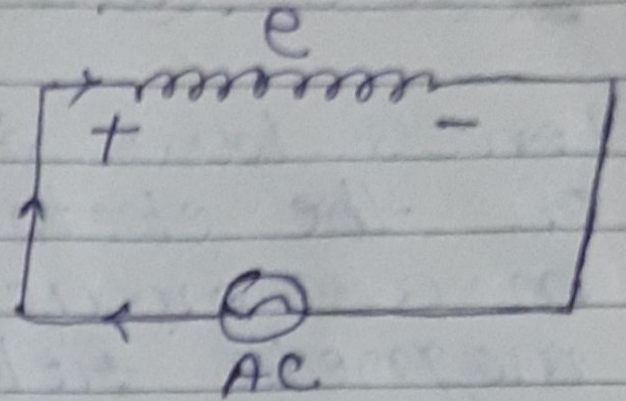
$$\phi = L \cdot I$$

$I$  = current

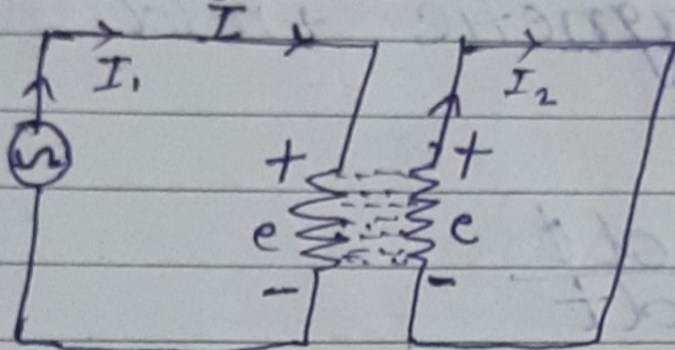
$L$  = Inductance of the coil (Henry).

$$e = -N \frac{d\phi}{dt}$$

$$e = -N \frac{d(LI)}{dt}$$



\* Mutual inductor:-



If a coil placed near to the changing carrying coil then flux cut through it as a result an emf is induced.

$$e = -M \frac{dI_1}{dt}$$

$m =$  mutual induction

It's SI unit is Henry.

\* Absolute permeability ( $\mu_0$ ) :-

permeability is the measure of the ability of the material to allow the formation of magnetic lines of force within magnetic field.

$$\mu_0 = 4\pi \times 10^{-2} \text{ H/M}$$

\* ( $\mu_r$ ) Relative permeability :-

It is the ratio of permeability of the material to the absolute permeability.

Dimensionless and unitless this ability.

\* Reactance :-

The resistance offered by the capacitor or inductor is known as Reactance. It depends on frequency.

\* Inductive Reactance :-

The reactance offered by the inductor is known as inductive Reactance. It is represented by  $X_L$

$$X_L = \omega L$$

$$X_L = 2\pi fL$$

where

$$\omega = 2\pi f$$

$f$  = frequency (50 Hz)

$L$  = inductance (H).

\* Capacitive Reactance :-

The reactance offered by the capacitor is known as capacitive reactance.

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C}$$

where,

$$\omega = 2\pi f$$

$f$  = frequency

$C$  = capacitance (F).

\* current :- The flow of electric charge is known as electric current.

$$I = \frac{d\phi}{dt}$$

S.I unit  $\rightarrow$  Ampere

where.

$\phi$  = charge

$t$  = time.

\* power factor (P.f) :-

cos sign

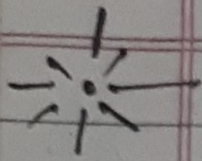
The ~~cosine~~ angle between voltage and current is known as power factor.

OR

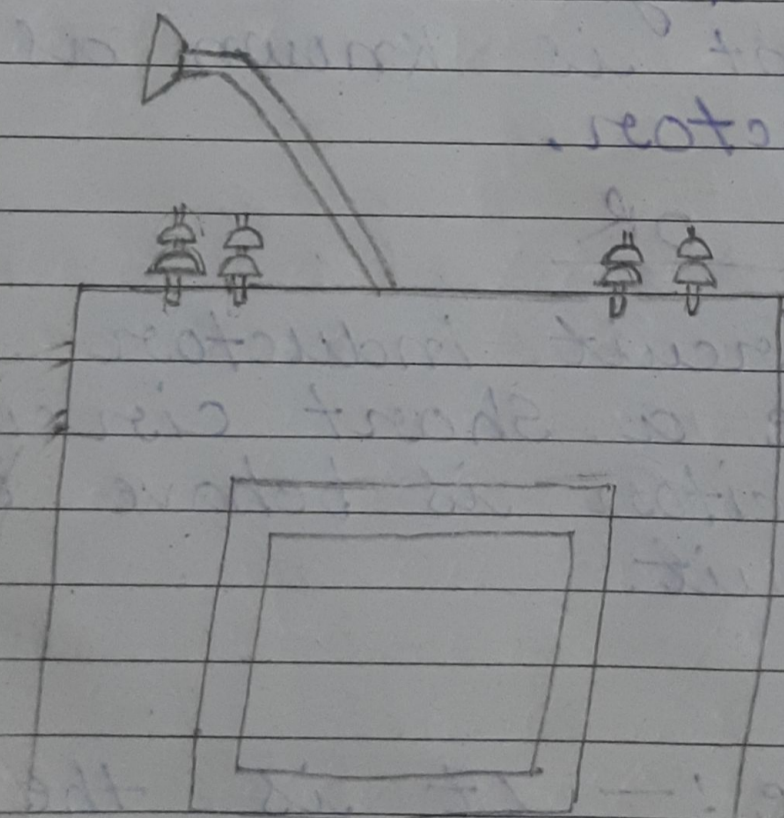
In DC circuit inductor is behave like a short circuit and capacitor is behave like a open circuit.

\* Impedance :- It is the equivalent resistance offered by an electric circuit (AC circuit) is known as Impedance. It is represented by 'z'

$$Z = \sqrt{R^2 + X^2}$$



Transformer:- Transformer \*  
transferred the electrical  
energy from one electric circuit  
to another electric circuit  
without changing the frequency  
and power. OR Transformer is  
an electro magnetic energy  
conversion static device it is  
commonly used in electrical  
power system and distribution  
system.



\* primary side :- That side of Transformer in which source or input or excitation is applied is known as primary side

\* secondary side :- That side of transformer in which load is connected.

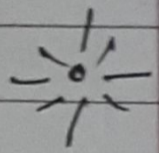
\* construction of Transformer :-

A Transformer is mainly consist of primary winding, secondary winding and core with the increase in the size or capacity of the transformer it also needs other part such as suitable tank, breather, conservator, explosion vent, buchholz relay and busing.

\* core :- Generally it is made up laminated silicon steel it provide low reluctance path and minimize eddy current loss.

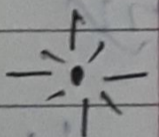


windings :- The coils forming the primary and secondary winding at transformer would be the well insulated copper (conductor) in the form of wire



Transformer tank :-

Transformer tank protect the transformer from moisture and other external distribution. It is made up of metallic material.



conservator tank :- The main function of conservator tank is to provide extra space to accommodate the transformer oil during oil expansion. It is a cylindrical tank maintained on the top of the transformer. It generally half filled transformer oil.

OR

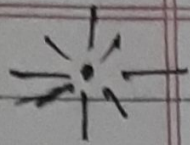
The main function of conservator tank to provide extra space is to expand the transformer oil during oil expansion due to

heating.

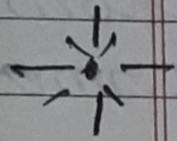
\* Breather :- The main function of breather is to prevent ~~moisture~~ (protect) moisture to enter the transformer during the breathing cycle of transformer it contain the silica gel that observe the moisture from the air and prevent transformer oil.

\* Buchholz relay :- The main function of buchholz relay is to protect the transformer from different internal fault. It detects the occurrence of fault and generate the alarm circuit. It is present in the main tank and conservation tank.

\* Cooling tube :- The main function of cooling tube is to transfer transformer heat from the transformer coil and core to the environment. The heated transformer oil circulates through the cooling tubes, where the heat radiates out.



Top charge :- The main function of top charge is to regulate the transformer output voltage by altering the number of turn in one winding and there by changing the turn ratio of transformer.



Explosion vent :- The main function of explosion vent is to provide protection against excessive pressure build up in the transformer during heavy internal fault.

\* classification of substances according to  $\mu_r$  :-

(i) Non magnetic substances :- ( $\mu_r = 1$ )

eg:- Air, cotton, glass, wood, plastic, mica, rubber etc.

(ii) Magnetic substances :-

(a) Diamagnetic ( $\mu_r < 1$ )

eg:- Antimony, Bismuth, copper, quartz, water, etc.

(b) paramagnetic ( $\mu_r > 1$ )

eg:- Aluminium, chromium, manganese, lithium, platinum, etc.

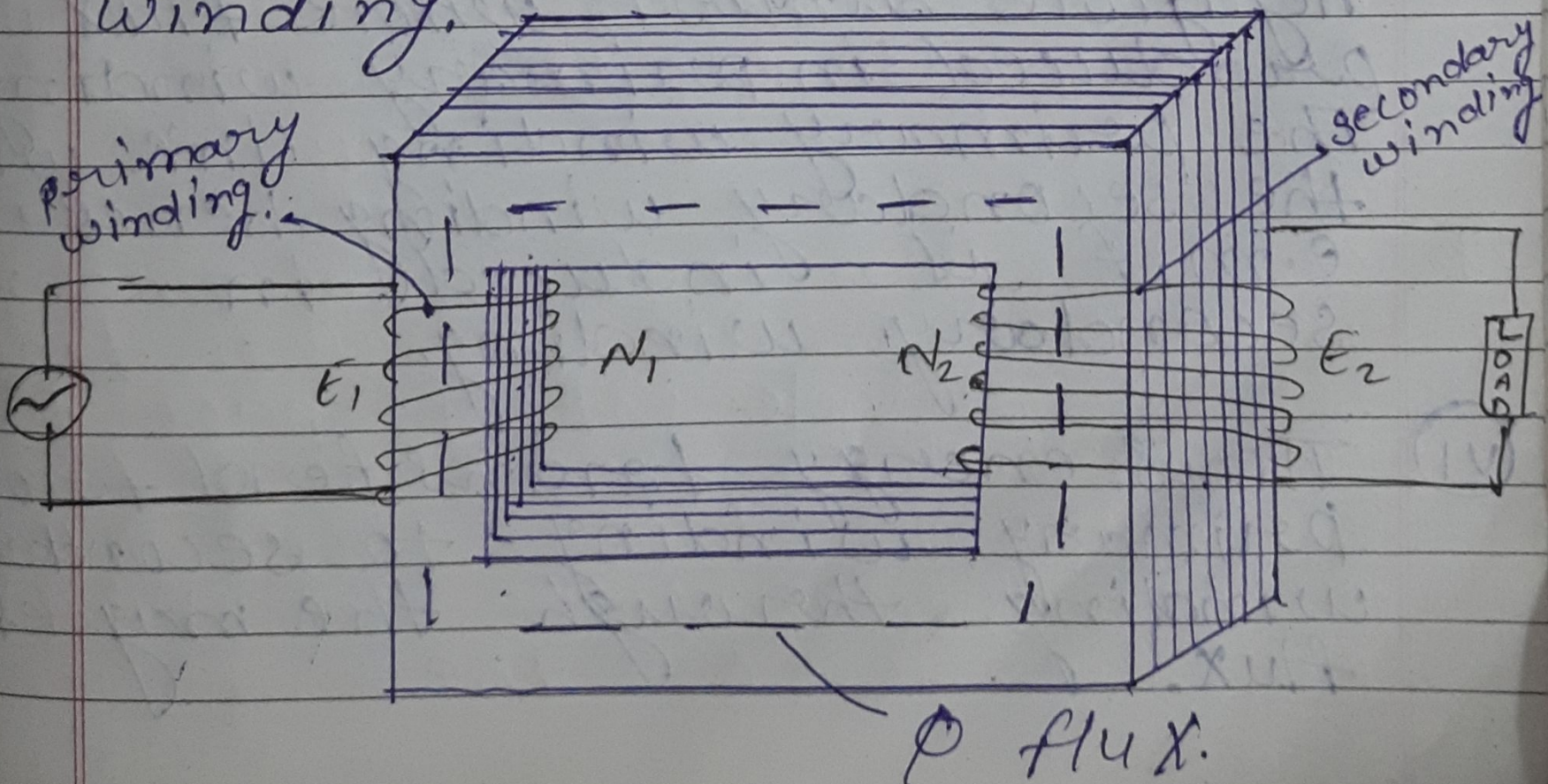
(c) ferromagnetic ( $\mu_r \gg 1$ )

eg:- Iron, cobalt, Nickel and their alloys.

\* working principle of transformer :-

(i) The transformer is static piece of device by means of which an electric power transferred from one circuit to another circuit with change in frequency.

(ii) A transformer operates on the principle of mutual inductance between two inductively coupled coils. The winding in which electrical energy is fed is called primary winding and the other form energy is drawn out is called secondary winding.



- (iii) The primary winding has  $N_1$  number of turns, while the secondary winding has  $N_2$  number of turns. The basic transformer and its symbol is shown (A.1).
- (iv) When an alternating voltage  $V_1$  is applied to primary, an alternating current  $I_1$  flows in it producing alternating flux in the core. According to Faraday's law of electromagnetic induction, e.m.f. is induced in the primary winding.
- (v) Assume leakage flux to be negligible, almost whole flux produced in primary winding links with the secondary winding hence, e.m.f. is induced in secondary winding.
- (vi) Thus energy is transferred from primary winding to secondary winding through the magnetic flux.

\* Derive e.m.f equation, and explain transformation ratio.

Let the flux of any instant

$$\phi = \phi_m \sin \omega t \quad \text{--- (i)}$$

where,

$\phi_m$  = maximum flux.

Now,

assume Number of turns of the winding is  $N$

$\therefore$  from Faraday's law

$$e = -N \frac{d\phi}{dt}$$

$$e = -N \frac{d(\phi_m \sin \omega t)}{dt}$$

$$e = -N \phi_m \frac{d(\sin \omega t)}{dt}$$

$$e = -N \phi_m \frac{d \sin \omega t}{\sin \omega t} \times \frac{d \omega t}{dt}$$

$$e = -N \phi_m \cos \omega t \cdot \omega$$

$$\boxed{e = -N \phi_m \omega \cos \omega t}$$

$$e = N \phi_m \omega (-\cos \omega t)$$

$$e = N \phi_m \omega \left[ \sin(\omega t - \pi/2) \right]$$

$$e = N \phi_m \omega \sin(\omega t - \pi/2)$$

Let, ~~em~~

$$e_m = N \phi_m \omega$$

$$e_{rms} = \frac{e_m}{\sqrt{2}}$$

$$e_{rms} = \frac{N \phi_m \omega}{\sqrt{2}}$$

$$e_{rms} = \frac{\omega}{\sqrt{2}} N \phi_m$$

$$e_{rms} = \frac{2\pi f}{\sqrt{2}} N \phi_m \quad [\omega = 2\pi f]$$

$$e_{rms} = \frac{2\pi}{\sqrt{2}} N \phi_m f$$

$$\boxed{e_{rms} = 4.44 \phi_m f N} \quad \text{--- (11)}$$

where,

$\phi_m$  = maximum flux

$f$  = frequency

$N$  = number of turns.

for primary winding number of turns is  $N_1$

$$e_{1\text{rms}} = 4.44 \phi_m f N_1 \quad \text{--- (iii)}$$

for secondary winding number of turns is  $N_2$

$$e_{2\text{rms}} = 4.44 \phi_m f N_2 \quad \text{--- (iv)}$$

Now, divided eq<sup>n</sup> (iii) and (iv)

$$e_{1\text{rms}} = E_1, \quad e_{2\text{rms}} = E_2$$

then

$$\frac{E_1}{E_2} = \frac{4.44 \phi_m f N_1}{4.44 \phi_m f N_2}$$

$$\boxed{\frac{E_1}{E_2} = \frac{N_1}{N_2}} \quad \text{or,} \quad \boxed{\frac{E_2}{E_1} = \frac{N_2}{N_1}}$$

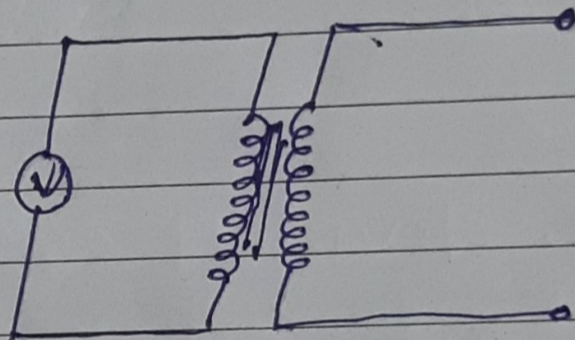
Transformation ratio.

# Glosses of transformer

## \* Transformer on no-load:-

A transformer is said to be on no load when the secondary winding is open circuited. The secondary current is zero. When an alternating voltage is applied to the primary a small current ( $I_0$ ) flows in the primary. This current  $I_0$  is called the no load current of transformer.

$I_0$  = no load current



$I_0 \rightarrow 2$  to  $5\%$  of rated current.

- It is made up of two components of  $I_m$  and  $I_w$ .

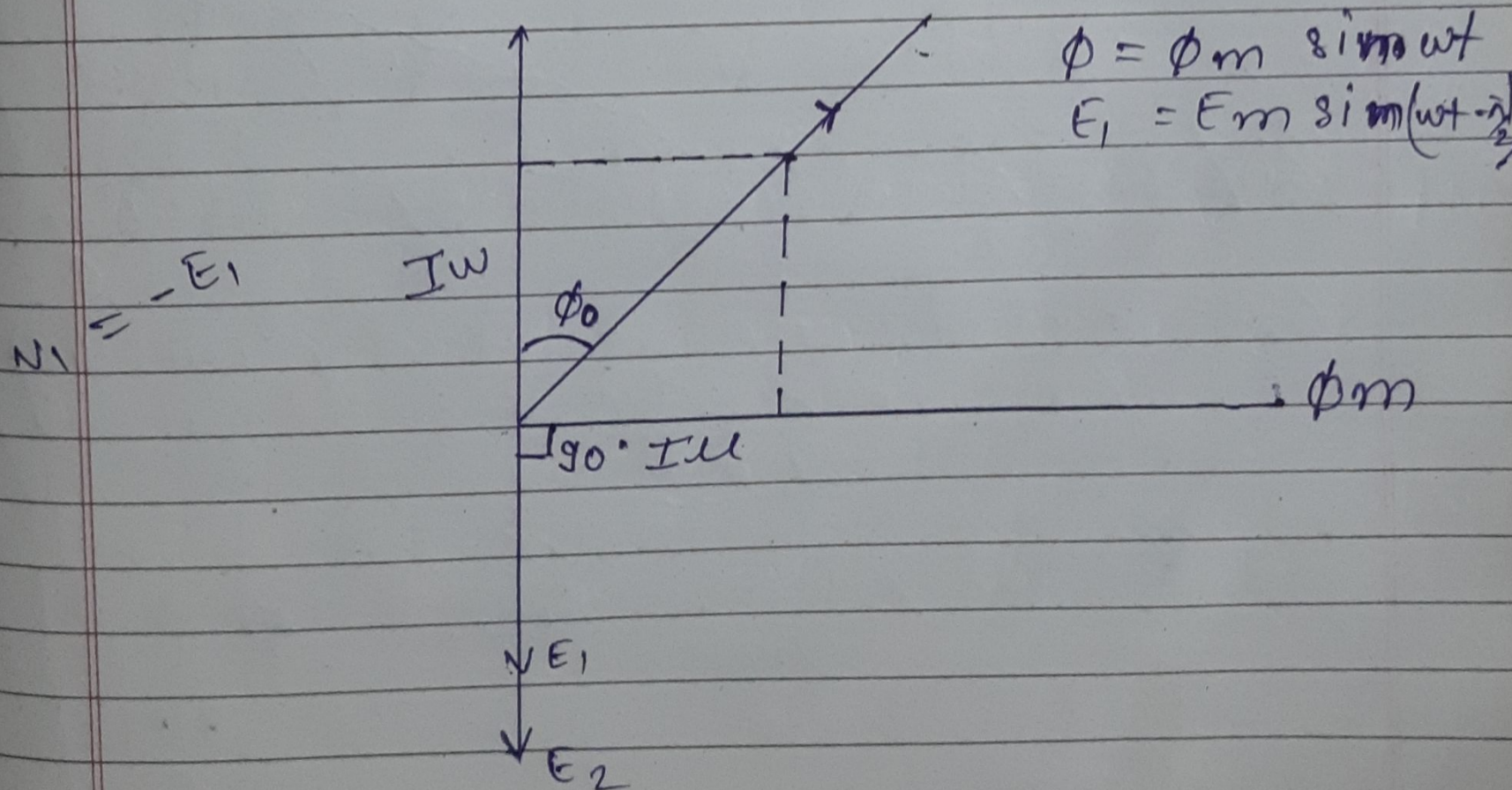
The component  $I_m$  is called the magnetizing component. It magnetizes the core. In other words, it sets up a flux in the core and hence for  $I_m$  is in phase with  $\phi_m$ .

The current  $I_m$  is also called reactive, wattless component of no load current.

The component  $I_w$  supplies is the hysteresis and eddy current losses. In the core. The current  $I_w$  is called the active component or wattful component of no load current. It is in phase with applied voltage  $V_1$ .

The no load current is 2 to 5% of rated or full load current of the transformer.

★ phasor diagram of transformer at no load:-



$$I_M = I_0 \sin \phi_0$$

$$I_W = I_0 \cos \phi_0$$

$$I_0 = \sqrt{I_M^2 + I_W^2}$$

power factor at no load =

$$\cos \phi_0 = \frac{I_M}{I_0}$$

$$\text{core loss} = V_1 I_0 \cos \phi_0$$

$$= V_1 I_M$$

(watt)

Ideal transformer:-

An Ideal transformer is an imaginary transformer which has the following properties:-

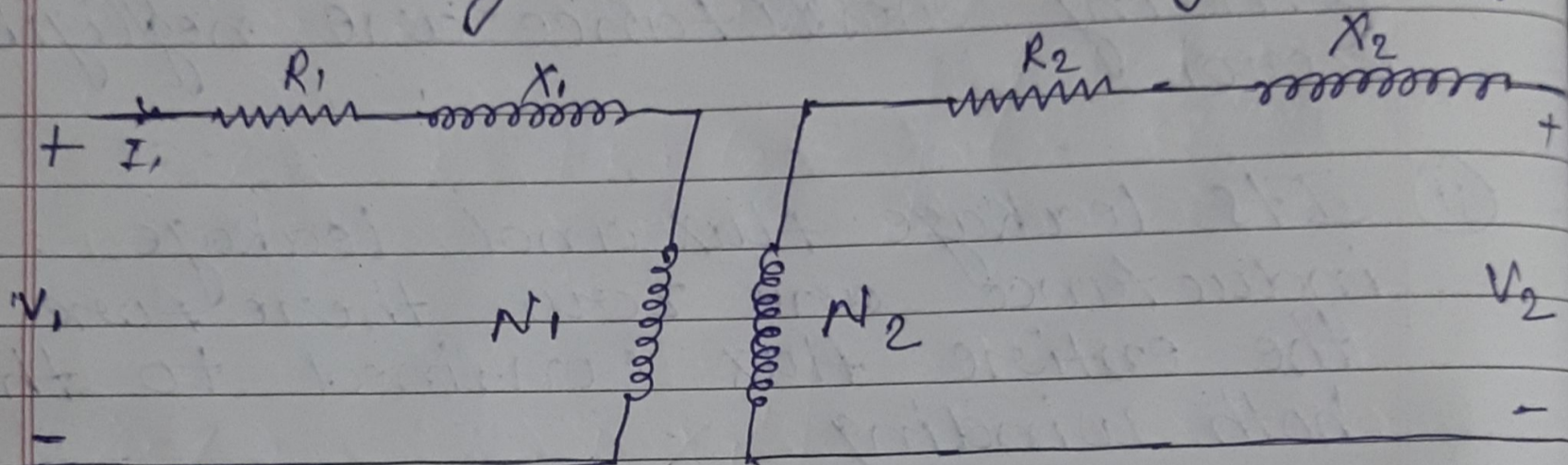
- (i) Its primary and secondary winding resistance are negligible (zero)
- (ii) Its leakage flux and leakage inductance are zero therefore the entire flux confined to the both winding
- (iii) There are no losses due to resistance, hysteresis and eddy current loss therefore the efficiency of Ideal transformer 100%.

$$\text{efficiency } (\eta) \% = \frac{\text{output}}{\text{input}} \times 100$$

$$\begin{aligned} \text{Input} &= \text{output} + \text{losses} \\ &= \text{output} + P_i + P_w \\ \text{output} &:= \text{input} - \text{losses} \\ &= \text{input} \end{aligned}$$

## \* winding resistance:-

An ideal transformer is supposed to have no resistance. But in actual transformer (practical transformer) there is always some resistance of primary and secondary winding.



where

$R_1$  = Resistance of primary winding

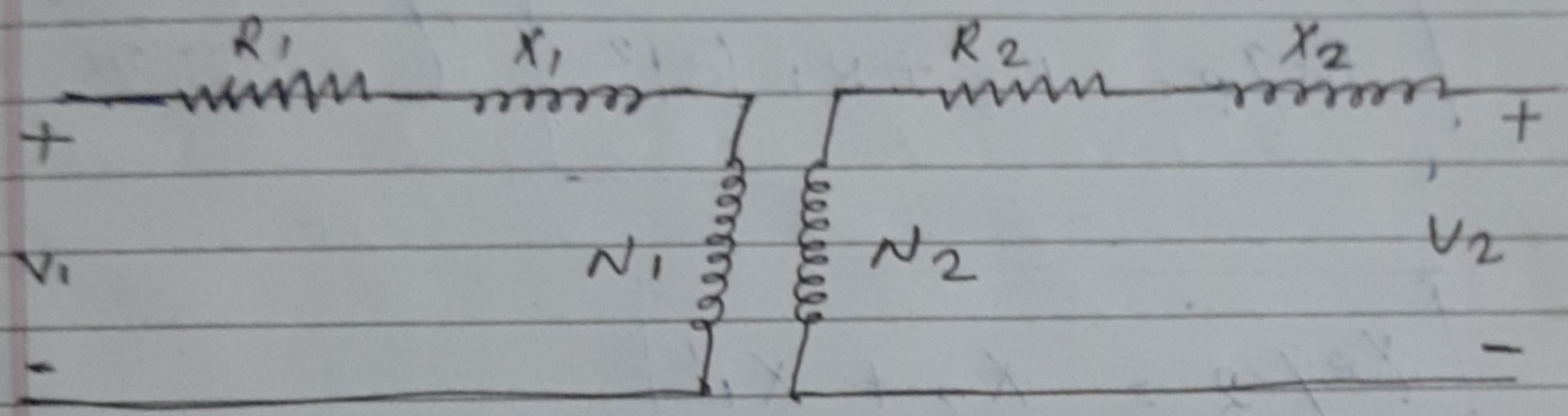
$R_2$  = Resistance of secondary winding

$X_1$  = Reactance of primary winding

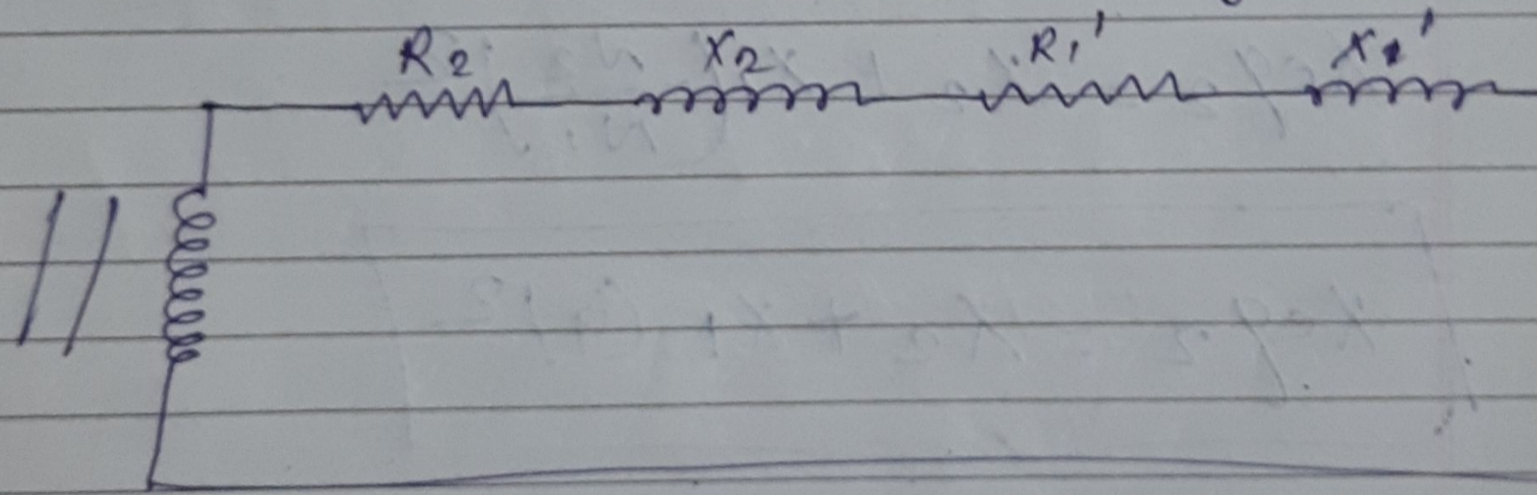
$X_2$  = Reactance of secondary winding.

\* Find referred values of resistance and reactance of transformer:-

- $R_1' \rightarrow R_1$  referred to secondary side
- $R_2' \rightarrow R_2$  referred to primary side
- $X_1' \rightarrow X_1$  referred to secondary side
- $X_2' \rightarrow X_2$  referred to primary side



$R_1, X_1$  referred to secondary side



$$R_1' = R_1 \left( \frac{N_2}{N_1} \right)^2$$

$$X_1' = X_1 \left( \frac{N_2}{N_1} \right)^2$$

$$R_{eq_2} = R_2 + R_1'$$

$$= R_2 + R_1 \left( \frac{N_2}{N_1} \right)^2$$

$$R_{eq_2} = R_2 + R_1 (a)^2$$

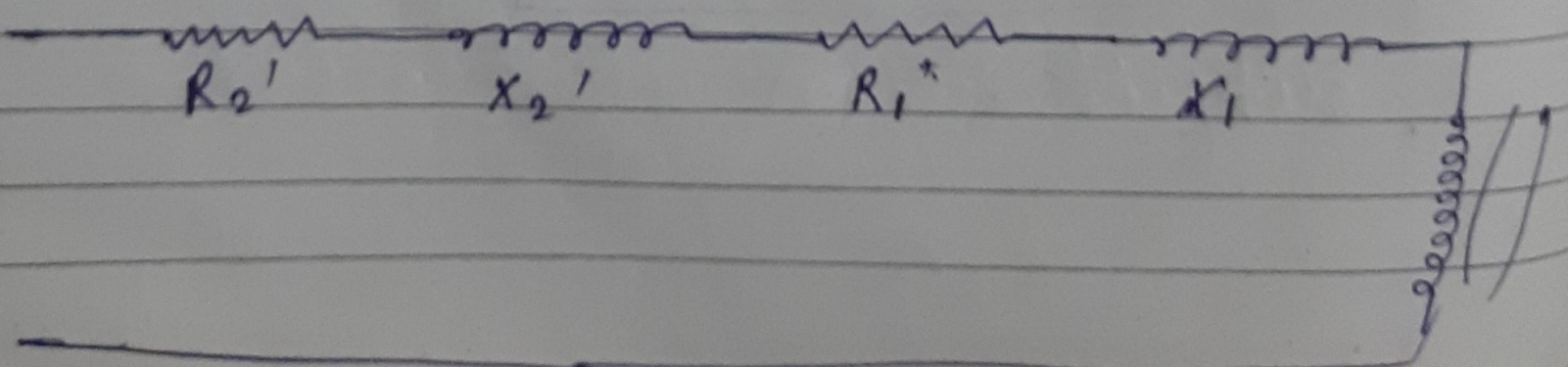
$a = \pm$  transformation ratio

$$X_{eq_2} = X_2 + X_1'$$

$$X_{eq_2} = X_2 + X_1 \left( \frac{N_2}{N_1} \right)^2$$

$$X_{eq_2} = X_2 + X_1 (a)^2$$

\*  $R_2, X_2$  Referred to primary side.



$$R_2' = R_2 \left( \frac{N_1}{N_2} \right)^2$$

$$Z_{eq,2} = \sqrt{R_{S2}^2 + X_{S2}^2}$$

$$X_2' = X_2 \left( \frac{N_1}{N_2} \right)^2$$

$$R_{eq,1} = R_1 + R_2'$$

$$R_{eq,1} = R_1 + R_2 \left( \frac{N_1}{N_2} \right)^2$$

$$R_{eq,1} = R_1 + R_2 \left( \frac{1}{a^2} \right)$$

$$X_{eq,1} = X_1 + X_2'$$

$$= X_1 + X_2 \left( \frac{N_1}{N_2} \right)^2$$

$$X_{eq,1} = X_1 + X_2 \left( \frac{1}{a^2} \right)$$

$$Z_{eq,1} = \sqrt{R_{p1}^2 + X_{p1}^2}$$

Impedance

# 9 Numericals

Q:- A 200 KVA single phase transformer with the voltage ratio of 6350/600V has the following winding resistance and reactance

$$R_1 = 1.56 \Omega \quad R_2 = 0.016 \Omega$$
$$X_1 = 4.67 \Omega \quad X_2 = 0.048 \Omega$$

Calculate the resistance and reactance of the transformer referred to high voltage winding.

given →

$$V_1 = 6350V \quad V_2 = 600V$$
$$R_1 = 1.56 \Omega \quad R_2 = 0.016 \Omega$$
$$X_1 = 4.67 \Omega \quad X_2 = 0.048 \Omega$$

$$R_2' = R_2 \left( \frac{N_1}{N_2} \right)^2 \left[ \frac{N_1}{N_2} = \frac{V_1}{V_2} \right]$$
$$= \frac{0.016 \times (6350)^2}{1000 \times (600)^2}$$

$$\frac{16}{1000} \times \frac{403225}{3600}$$

$$\frac{6451.6}{3600000} = 1.79$$

$$R_e' = R_1 + R_2'$$

$$= 1.56 + 1.79$$

$$= 3.35 \Omega$$

$$R_1' = R_1 \left( \frac{N_2}{N_1} \right)^2$$

$$\frac{1.56}{100} \left( \frac{600}{6350} \right)^2$$

$$\frac{1.56}{100} \times \frac{3600}{403225}$$

$$\frac{5616}{403225}$$

$$X_2' = X_2 \left( \frac{N_1}{N_2} \right)^2$$

$$\frac{0.048}{1000} \times \left( \frac{6350}{600} \right)^2$$

$$\frac{48}{1000} \times \frac{403225}{3600}$$

$$\frac{19354800}{3600000} = 5.37$$

$$X_{e1} = X_1 + X_2'$$

$$= 4.67 + 5.37$$

$$= 10.04$$

## \* Losses of transformer:-

- (i) copper loss or winding loss
- (ii) Iron loss  $\left\{ \begin{array}{l} \rightarrow \text{Hysteresis loss} \\ \rightarrow \text{eddy current loss} \end{array} \right.$  or core loss
- (iii) stray loss or flux loss
- (iv) dielectric loss.

(i) Copper loss or winding loss or resistive loss or variable loss

Resistive loss is the power loss in a transformer caused due to the ohmic resistance of copper wire used to make the winding the power is dissipated in the form of heat due to the electric current in the conductors of transformer primary & secondary winding these losses are also called copper loss or ohmic loss.

## ① Iron loss or core loss:-

Core of the transformer is the one that links both like primary and secondary winding by magnetic induction. The losses that occurs in the magnetic core are called core loss in transformer.

\* There are two main types of iron loss

- ① Hysteresis loss
- ② eddy current loss.

### ① Hysteresis losses:-

Hysteresis loss in a transformer occurs due to magnetization saturation in the core of the transformer. Magnetic materials in the core will eventually become magnetically saturated when they placed in a strong magnetic field such as the magnetic field generated by an AC current.

Hysteresis loss is caused by the magnetization and demagnetization of the core as current flows in the forward and reverse directions. As the magnetizing force (current) and magnetic flux increase,

\* stray losses :- stray losses refer to the heat losses that occurs in all transformer components except for the copper winding.

\* Dielectric losses :-

The power loss occurs in insulating materials like oil, solid insulation of the transformer etc is known as dielectric loss.

## Losses of transformer

$$P_i = P_m + P_e$$

$P_i \rightarrow$  Iron loss

$P_m \rightarrow$  Hysteresis loss

$P_e \rightarrow$  eddy current loss

$$P_m = K_m f B_m^x$$

$$P_e = K_e f^2 B_m^2$$

\*  $K_m \rightarrow$  proportionality constant which depends upon the volume and quality of the core materials!

\*  $K_e \rightarrow$  proportionality constant which depends upon the volume and quality of the core materials, thickness of the lamination

$B_m \rightarrow$  maximum flux density

$f \rightarrow$  frequency

$x \rightarrow$  load fraction.

$$P_n \propto f$$

$$P_n = af \quad \text{--- (i)}$$

$$P_e \propto f^2$$

$$P_e = bf^2 \quad \text{--- (ii)}$$

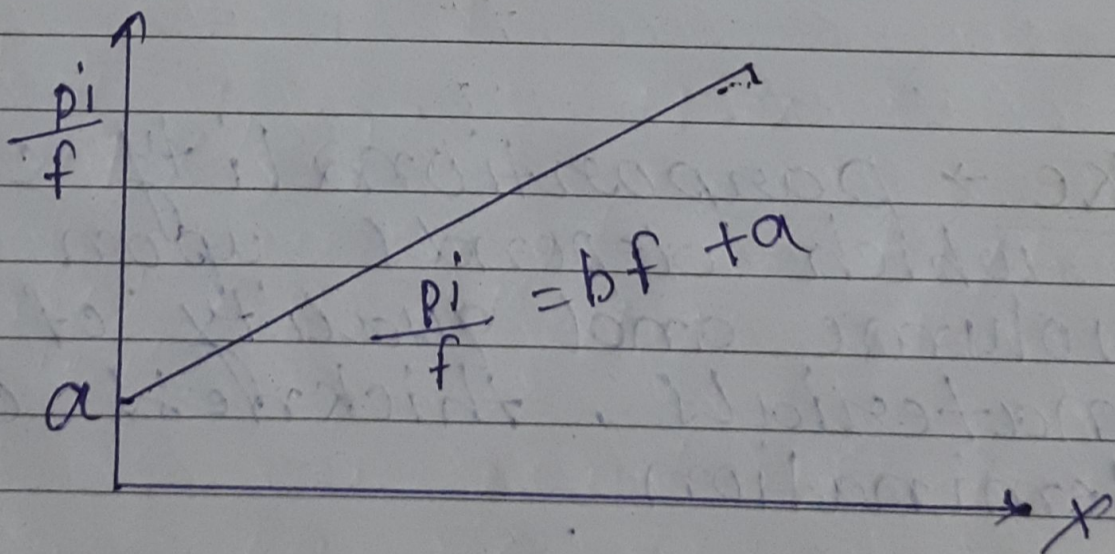
$$P_i = P_n + P_e$$

$$P_i = af + bf^2 \quad (\text{from (i) \& (ii)})$$

$$P_i = f(a + bf)$$

$$\frac{P_i}{f} = a + bf$$

$$\boxed{\frac{P_i}{f} = bf + a}$$



\* Total copper loss of transformer  
= primary winding copper loss  
+ secondary winding copper loss

$$P_c = I_1^2 R_1 + I_2^2 R_2$$

\* No-load losses :-

At no-load in transformer copper loss is very less because of no-load current is very small (2 to 5%) that's why ~~we~~ we consider only iron losses.

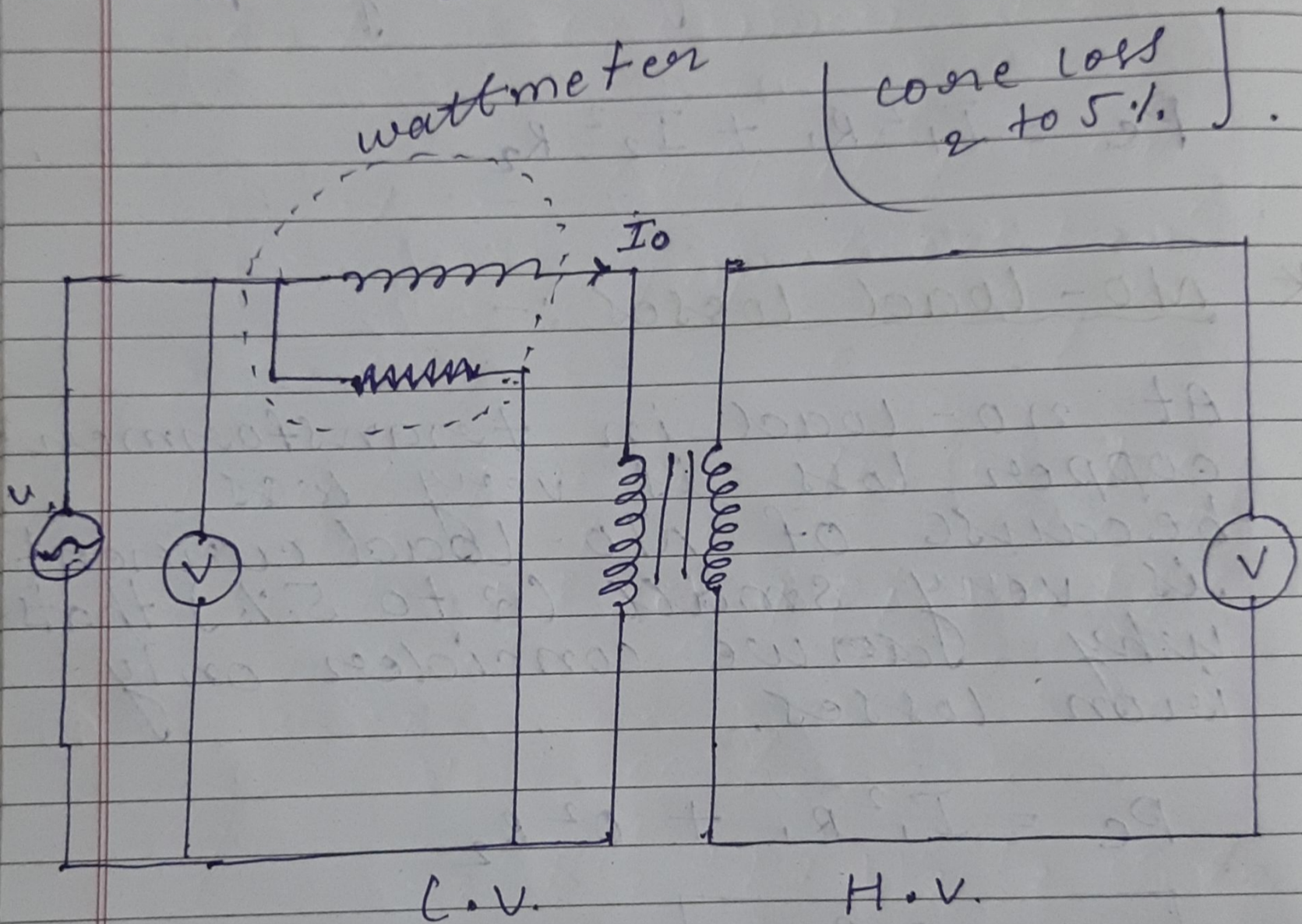
$$P_c = I_1^2 R_1 + 0^2 R_2$$

$$\boxed{P_c = I_1^2 R_1}$$

\* open circuit test :-

open circuit test are perform to determine the circuit constants, efficiency and regulation the transformer. These test gives

more accurate results than these obtained by taking measurement on fully loaded condition transformer



- L.V. side current is high as compareason to H.V. side
- H.V. side current is low as compareason to L.V. side

$$P_i = P_{i\text{iron}}$$

$$P_{i\text{iron}} = V_1 I_o \cos \phi_o$$

$$P = VI \cos \phi_0$$

- \* Ammeter reading = No load current ( $I_0$ )
- \* voltmeter reading = primary rated voltage ( $V_1$ )
- \* watt meter reading = iron or core loss ( $P_i$ )

\* Efficiency :- It is the ratio of output power to the input power of transformer is known as efficiency of the transformer.

$$\eta \% = \frac{\text{output power}}{\text{input power}} \times 100$$

$$\begin{aligned} \text{input power} &= \text{losses} + \text{output power} \\ &= I_2^2 R_{e2} + P_i + V_2 I_2 \cos \phi_2 \end{aligned}$$

$$\eta = \frac{V_2 I_2 \cos \phi_2}{I_2^2 R_{e2} + P_i + V_2 I_2 \cos \phi_2}$$

$$\eta = \frac{V_2 I_2 \cos \phi_2}{V_2 I_2 \cos \phi_2 + P_i + I_2^2 R_{e2}}$$

\* condition for maximum efficiency :-

$$\eta = \frac{V_2 I_2 \cos \phi_2}{V_2 I_2 \cos \phi_2 + P_i + I_2^2 R_{e2}}$$

$$\eta = \frac{V_2 \cos \phi_2}{V_2 \cos \phi_2 + \frac{P_i}{I_2} + I_2 R_{e2}}$$

for minimum value

$$\frac{d}{dI_2} \left[ V_2 \cos \phi_2 + \frac{P_i}{I_2} + I_2 R_{e2} \right] = 0$$

$$= 0 + P_i \left( \frac{-1}{I_2^2} \right) + R_{e2} = 0$$

$$P_i \left( \frac{-1}{I_2^2} \right) + R_{e2} = 0$$

$$\frac{-P_i}{I_2^2} + R_{e2} = 0$$

$$\frac{+P_i}{I_2^2} = +R_{e2}$$

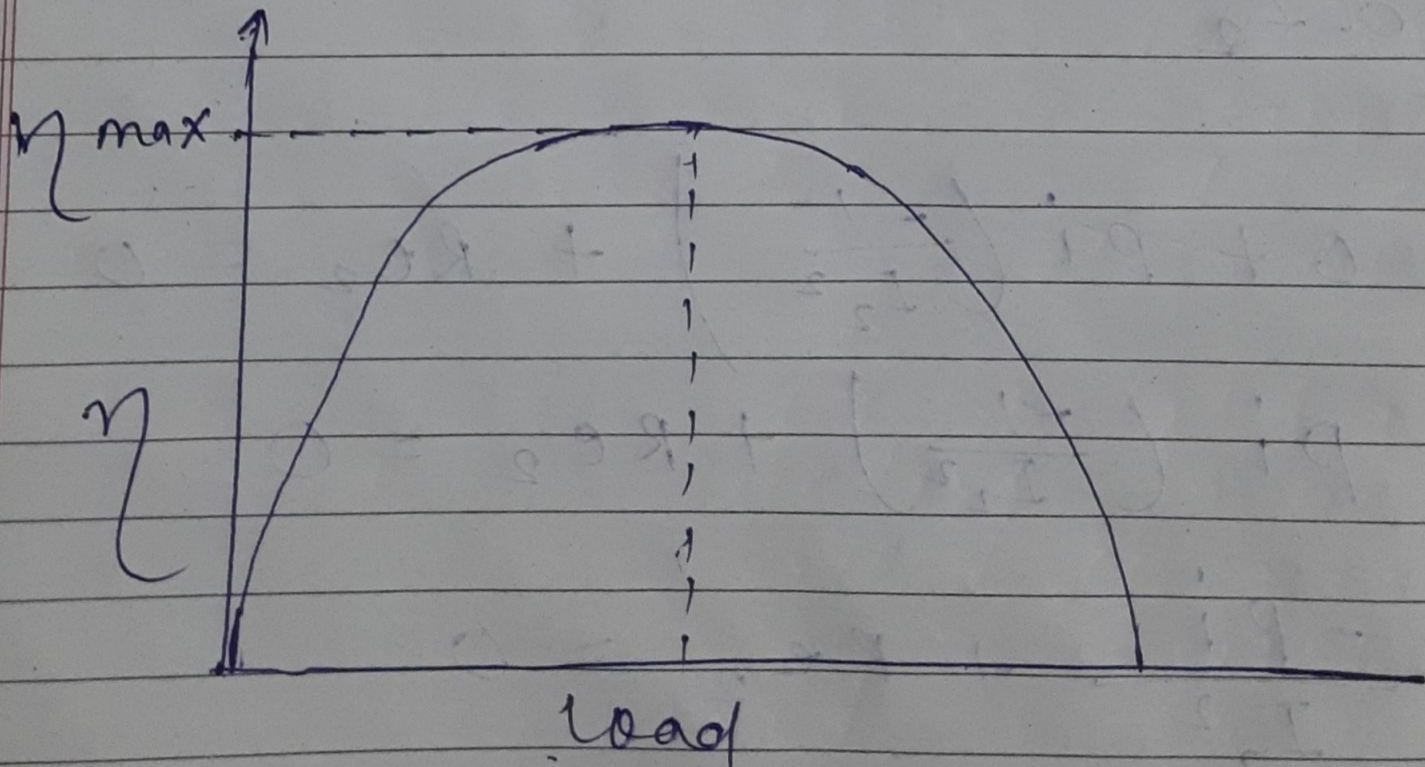
$$P_i = R_{e2} I_2^2$$

where

$P_i \Rightarrow$  iron loss (constant)

$I_2^2 R_{e2} \Rightarrow$  core loss (variable)

variable loss is equal to constant loss of the transformer then transformer work on maximum efficiency.



### \* All day efficiency :-

It is the ratio of output power over 24 hours to the input power over the 24 hours.

$$\text{all day } \eta = \frac{\text{output power over 24 hours}}{\text{input power over 24 hours}}$$

Q:- A 25 kVA, 2000/200V Transformer with iron and full load copper loss of 350 W and 400 W is load full at 0.85 p.f calculate the  $\eta$  of the transformer at this power factor

$$V_1 = 2000 \text{ V}, V_2 = 200 \text{ V}$$
$$P_i = 350 \text{ W}, P_{cu} = 400 \text{ W}$$

$$\cos \phi_2 = 0.85 \quad V_2 I_2 = 25 \times 10^3$$

$$\eta = \frac{V_2 I_2 \cos \phi_2}{V_2 I_2 \cos \phi_2 + P_i + I_2^2 R_{e2}}$$

$$= \frac{25 \times 10^3 \times 0.85}{25 \times 10^3 \times 0.85 + 350 \times 400}$$

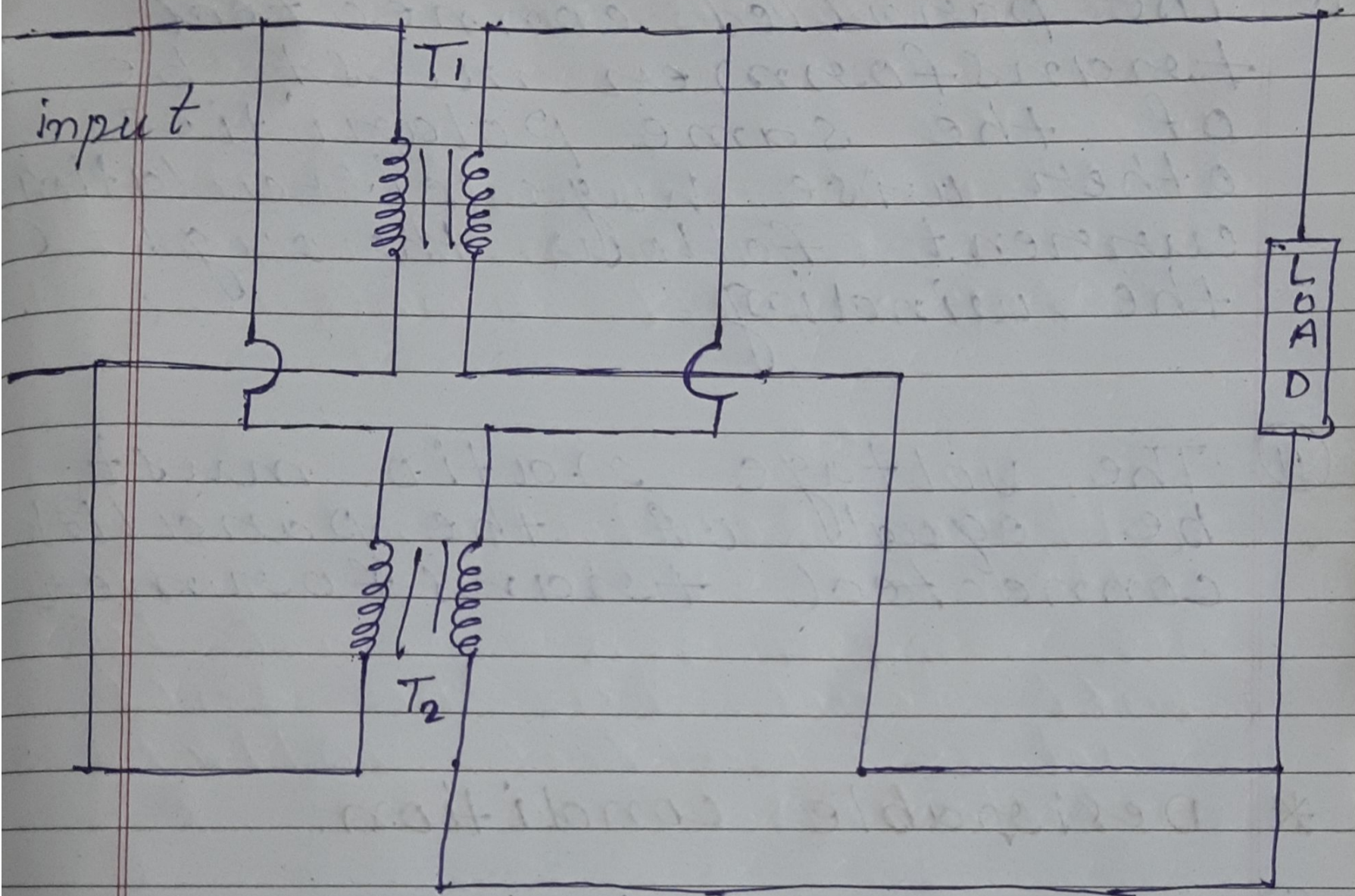
$$= \frac{21250}{22000}$$

$$\eta = 0.965$$

$$\eta \% = \frac{0.965}{1000} \times 1000$$

$$96.5\% \quad \text{Ans.}$$

\* parallel operation of single phase transformer.



when two or more transformers connected with same input (common) input (source) and their output are connected with same load then it is called parallel operation of single phase transformer.

\* condition for parallel operation :-

(i) The parallel connected transformer must be of the same polarities otherwise huge circulating current flows through the winding.

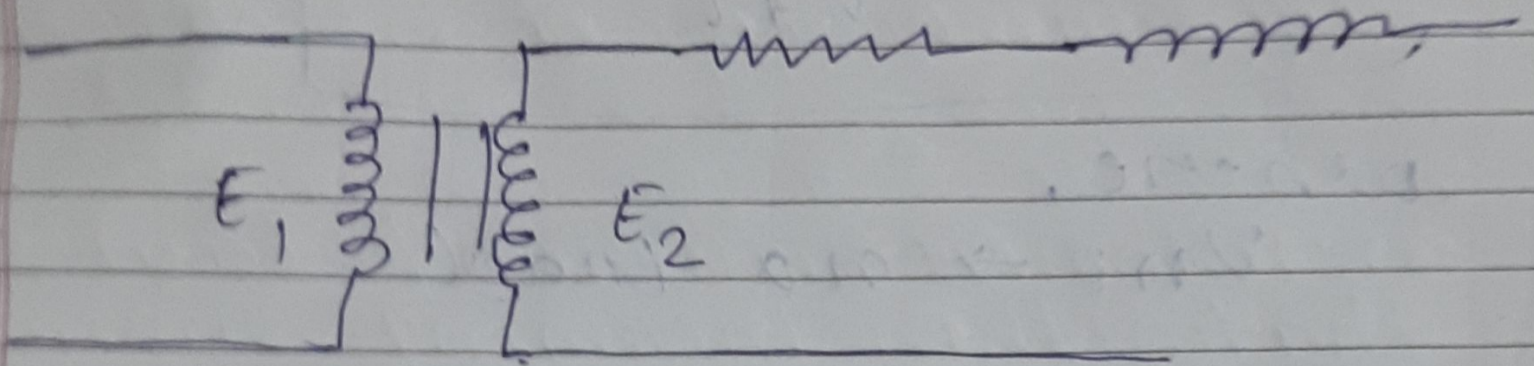
(ii) The voltage ratio must be equal of the parallel connected transformer.

\* Desirable condition.

(i) The ~~ratio~~ internal impedance of the parallel connected transformer should be equal.

(ii) The ratio of resistance to the inductive reactance of the parallel connected transformer should be same (equal).

\* Voltage regulation :-



Actually the transformer is designed to operate at constant voltage. But due to voltage drop by internal impedance of the transformer the output voltage of the transformer will get less. This parameter is known as voltage regulation.

$$V.R = \frac{V_{nl} - V_{fl}}{V_{fl}}$$

where,

$V_{nl} \rightarrow$  no load

$V_{fl} \rightarrow$  full load.

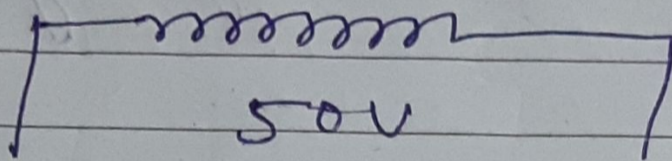
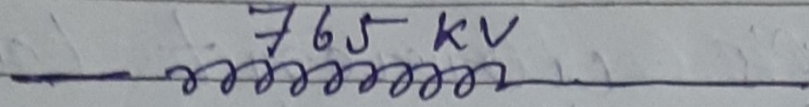
OR

Voltage Regulation is the ratio of voltage difference from no load to full load to the full load is called voltage regulation.

Voltage  $\uparrow \rightarrow$  step down  
current  $\uparrow \rightarrow$  step up

\* potential transformer:-

$$V_1 = \left( \frac{N_1}{N_2} \right) V_2$$



step down.

CT (current transformer)

CT connected of sense circuit

PT (potential transformer)

PT connected of parallel transformer.

## \* Ideal transformer

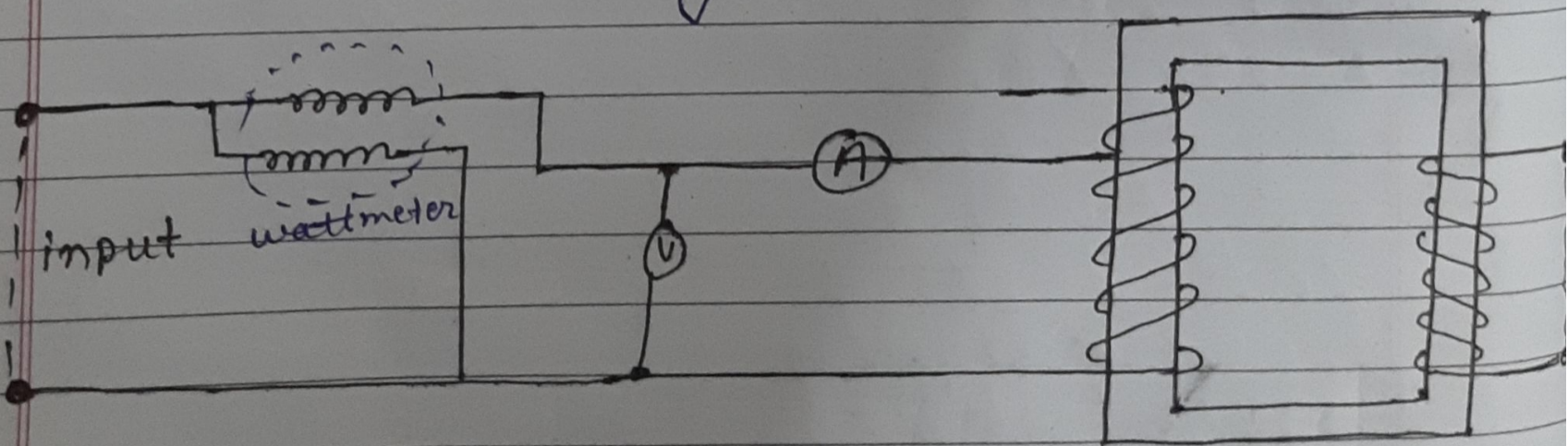
An ideal transformer is an imaginary transformer which has the following properties

- (i) Its primary and secondary winding resistance are negligible.
- (ii) Its leakage flux and leakage inductance are zero. The entire flux is confined to the core and links both windings.
- (iii) There are no losses due to resistance, hysteresis and eddy currents. Thus the efficiency  $\eta$  is 100%.

## \* short circuit test

In this test secondary winding is generally short circuited and primary is supplied with a small voltage and increased until full load current is flowing in this windings. This full load current is obtained on small percent of normal voltage.

As the applied voltage will be small percentage of its normal value, hence, the iron loss will be small, so it can be neglected. The wattmeter reading will give the copper losses and ammeter will show primary full load current.



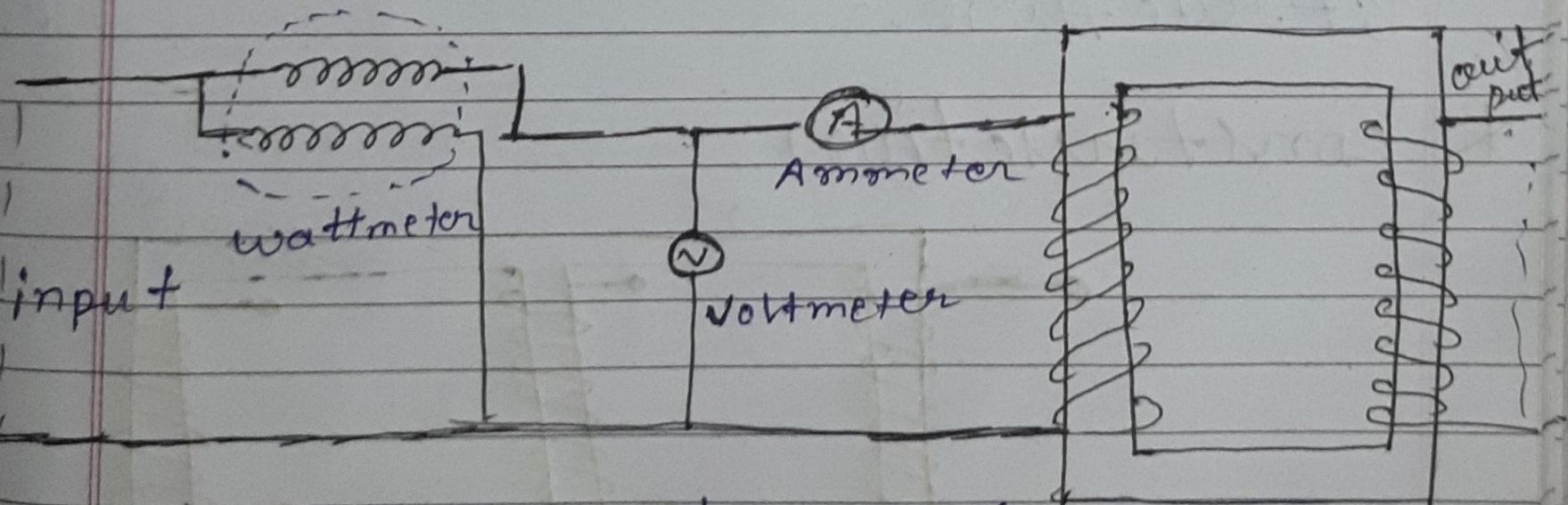
short circuit test

\* open circuit test :-

This test is used to calculate the iron losses of transformer in the no-load condition. Generally primary being supplied at normal voltage and frequency, and the secondary winding is left open circuit.

A wattmeter, voltmeter and Ammeter is connected to the primary side. Ammeter gives the no-load current and wattmeter show the no-load losses.

In the primary winding no-load current is negligible as compared to iron loss. Hence the wattmeter reading only show the iron losses.



Open circuit test.

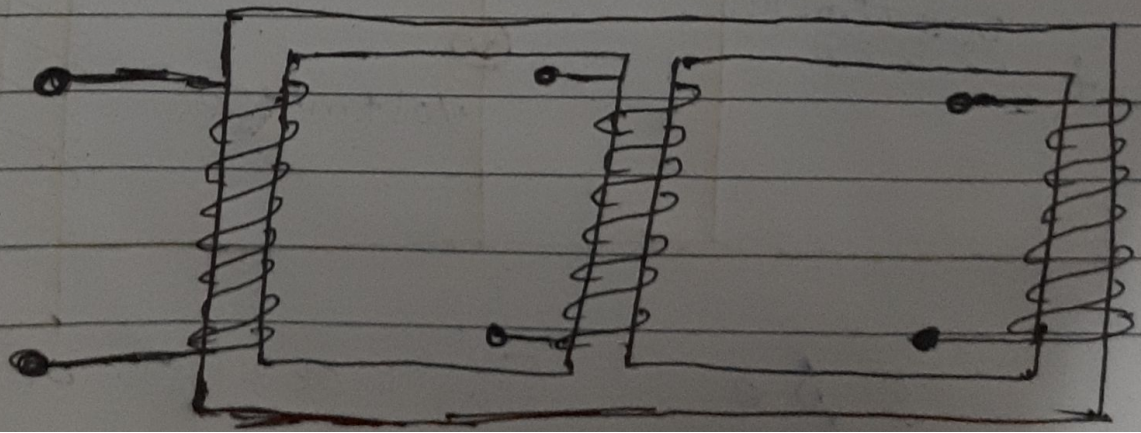
# Three-phase Transformer

\* A three-phase system is used to generate and transmit large amount of power. Three phase transformer are required to step-up or step down voltages in various stage of a power system network.

\* Transformer of 3- $\phi$  circuit can be constructed in one of the following ways:-

- The separate single phase transformer are suitably connected for 3- $\phi$  operation such an arrangement called a Three-phase bank of transformer
- A single three-phase transformer in which the cores and windings for all the three phases are combined in a single structure:-

\* construction



construction of the magnetic core of a 3- $\phi$  core type transformer may be understood by considering three single phase core type transformer positioned at  $120^\circ$  each other for simplicity only the primary winding is shown. If balanced 3- $\phi$  sinusoidal voltages are applied to the windings the flux  $\phi_0$ ,  $\phi_m$  and  $\phi_e$  also will be sinusoidal and balanced. If the three legs carrying this fluxes are merged. The total flux in the merged leg is 0. (zero).